The side squares all commute. The bottom square is anticommutative by the above. Thus, since all the vertical maps are injective, the top square is anticommutative as